

Inverse problem for the Earth's core evolution model

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Received 13 September 2020; accepted 17 September 2020; published 22 September 2020.

The size and the age of the inner core impose constraints in modeling of the Earth's core evolution. The origin of the solid core corresponds to the change in convection regime in the core and, correspondingly, to the change in the magnetic field behavior. Meanwhile the standard evolutionary models predict quite young inner core that is not supported by the palaeomagnetic observations, which claim existence of geomagnetic field older than 3 Gy. We solve the inverse problem and find parameters of the model with the inner core older than 3 Gy. **KEYWORDS:** Liquid core; thermal and compositional convection; geodynamo.

Citation: Reshetnyak, M. Yu. (2020), Inverse problem for the Earth's core evolution model, *Russ. J. Earth. Sci.*, 20, ES5007, doi:10.2205/2020ES000740.

1. Introduction

It is believed that the liquid core of the Earth, appeared soon after accretion of the planet, was all the time in the well-mixed state due to the turbulent convection, caused by the superadiabatic heat flux through the core-mantle boundary (CMB) [*Gubbins et al., 1979; Labrosse et al., 1997*]. The cooling of the mantle, and respectively, the liquid core, leads to the change of convection regime in the core at geological times. After some time the inner core (IC) appears in the center of the Earth and starts to grow due to solidification process. By now its radius $c_m = 1220$ km, is 0.35 from the radius of the liquid core. From the origin of IC the pure thermal convection is accompanied by the so-called compositional convection, concerned with solidification of IC.

Due to appearance of two additional energy fluxes at ICB, concerned with compositional convection: the flux of the light constituent and the latent heat

flux caused by solidification process, see for details [*Braginsky & Roberts, 1995*]), this kind of convection is three times stronger than the thermal one. As a result, it is supposed, that the origin of IC is the remarkable phenomenon in the history of the Earth, which should change the magnetic field generation essentially.

However, the palaeomagnetic observations do not recognize the IC birth, see review [*Reshetnyak and Pavlov, 2016*]. This phenomenon, named as the IC paradox [*Olson, 2013*], can be caused by various reasons, such as the pure knowledge of the initial conditions concerned with accretion, uncertainty in the physical properties of the liquid core under the high pressure, as well as the details of interaction of the liquid core with the mantle, the magnitude of the heat flux at CMB in particular. The more dramatic reason may be related to the specific of the palaeomagnetic observations, based on the assumption of predominance of the dipole field in the past. So far the modern geodynamo models mostly predict that frequent reversals of the field correspond to the non-dipole magnetic field spectrum [*Christensen and Aubert, 2006; Driscoll, 2016*], we can not exclude this possibility as well.

One of the possibilities to overcome this contradiction is to explore the whole realistic phase space of parameters. Further we firstly check sensitivity of IC evolution to variations of the crucial param-

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eters in the model and discuss underlying physical mechanisms. Secondly, we solve the inverse problem and find parameters, such as CMB heat flux, initial temperature in the center of the Earth, and the solidification temperature, which provide the best correspondence of the inner core's size and age with seismological and palaeomagnetic observations (further the term "inverse problem" is understood in the general sense of the word, namely tuning of the model parameters). For this aim the Monte-Carlo method was used.

2. Preliminary analysis. Direct problem

We start from the standard evolutionary model of the core developed in [Gubbins *et al.*, 1979], [Labrosse *et al.*, 1997], [Labrosse, 2003]. It is assumed, that initially the liquid core was fully convective. The mantle cooling led to appearance of IC, which size increased from that time significantly, and, perhaps, thermally stratified region near CMB.

The model is based on the large number of parameters and gives distributions of the density, gravity, pressure, temperature, and some other physical properties of the core as a function of the radius and time. Many of them can not be observed directly and should be tested against other theories. As for example, the heat flux at CMB, should be considered together with the processes in the mantle. The electrical and magnetic properties are subject of the geodynamo study. But there is one important exception: the model predicts appearance and growth of IC, which modern radius c_m is estimated by the seismological methods quite accurately.

Here we start our analysis by checking how variations of some particular parameter influence on c , provided all other parameters are constant and taken from [Reshetnyak, 2019], see also Appendix and the Table 3 there.

The other quantity we follow is the birth time of IC a , counted from the end of accretion. It can not be estimated directly from observations, however we will discuss its relation to the geomagnetic observations further.

So far cooling of the core is caused by the heat flux at CMB, we start our analysis from dependency of IC growth on this quantity. As was al-

ready mentioned, the heat flux can not be measured directly and its magnitude is very uncertain. The most reasonable estimates follow from capability of convection to generate the magnetic field. The pioneer works, based on the simple structures of the large-scale geomagnetic field [Gubbins *et al.*, 1979], [Buffett, 2002] gave the lower estimate of the net heat flux at CMB $Q \sim 2$ TW. Taking into account 3D geodynamo modeling results, which let estimate input of the toroidal and the small-scale counterparts of the magnetic field, increased estimate up to $Q \sim 10 \div 20$ TW [Calderwood *et al.*, 2003].

Having in mind the above estimates in order of magnitude we introduce the prescribed density flux at CMB as follows $q_b = q_b^\circ(1 - 0.18t/A)$, where $q_b = Q/(4\pi r_{CMB}^2)$, $r_{CMB} = 3480$ km is the outer core radius, $A = 4.5$ Gy is the age of the liquid core, and time t in units of Gy. The resulted IC radius c at $t = 4.5$ Gy, and the time a when IC appeared, are shown in Figure 1 (upper plane). The range of q_b° corresponds to the net heat flux Q range at CMB [12–18] TW. The middle value $q_b^\circ = 0.075$ mW/m² corresponds to 15 TW, used in [Labrosse *et al.*, 1997]. The increase of cooling forces solidification process and as a result c increases, and IC appears faster (small a). The less a the older is IC. Its age, measured in Gy, is $4.5 - a$. Summarizing, we conclude that increase of q_b in the range $(6 \div 9) 10^{-2}$ mW/m² leads to increase of IC radius in the range $(0.84 \div 1.4) 10^3$ km and decrease of a from 3.8 Gy to 2.5 Gy.

The next parameter is the initial temperature at $t = 0$ in the center of the liquid core T_o . So far it is assumed that initially core was fully liquid, T_o should be larger than the solidification temperature in the center T_s° . The estimate of T_o is quite uncertain and can reach 10000 K [Rubie *et al.*, 2011]. We adopt more moderate estimate ~ 6000 K, used in [Labrosse *et al.*, 1997], [Reshetnyak, 2019]. Variations of c and a are shown in Figure 1 (middle plane). The higher is the initial temperature T_o in the center of the Earth the younger is IC, and the smaller is its size. For $T_o > 6400$ K the core should still be fully liquid.

The last parameter we consider here is the temperature of solidification T_s° in the center of the Earth. Its estimate has been revised in favor of the higher values from ~ 5270 K [Labrosse *et al.*, 1997] to $5400 \div 5700$ K [Alf e *et al.*, 2007], see in more details [Nimmo, 2007]. Dependencies of c and a ,

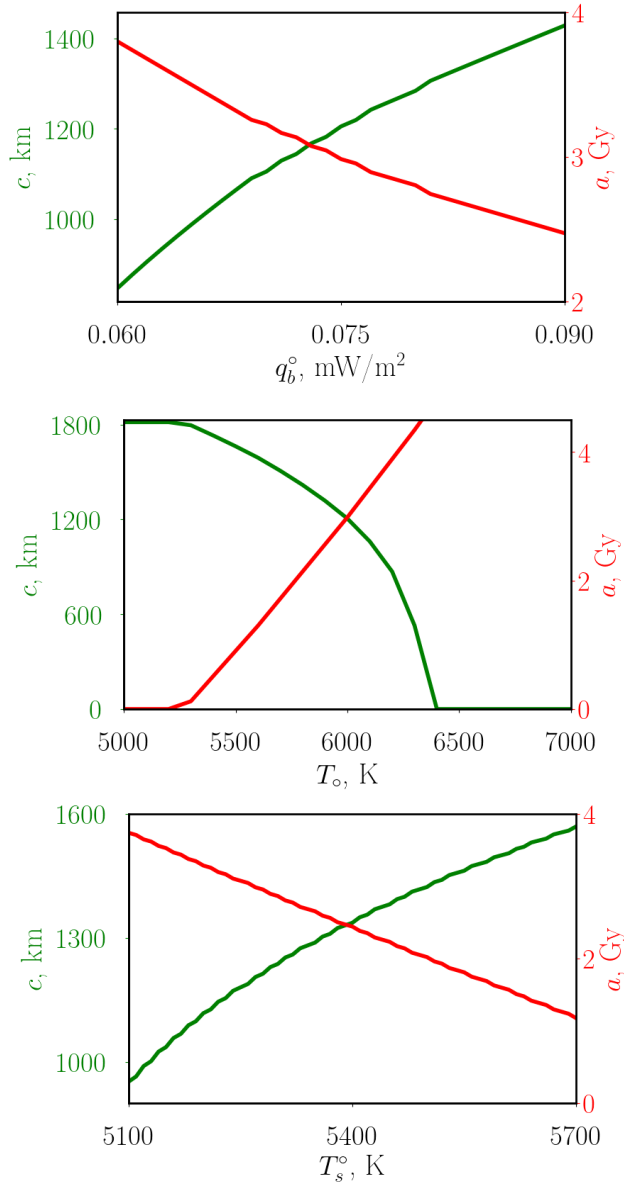


Figure 1. Dependence of the modern IC radius c and IC birth time a on q_b^o (the upper plane), T_o (the middle plane), T_s^o (the lower plane)

as it is expected, see Figure 1 (lower plane), are quite opposite to the previous case with T_o : increase of T_s^o leads to increase of IC size and IC becomes older.

As we can see variations of these three parameters can change IC size and age in wide ranges. These variations cover the acceptable size of IC, as well as predict existence of the quite old IC. The latter reconcile IC evolution with the palaeomagnetic observations, which do not recognize any dramatic change in the geomagnetic field [Reshetnyak and Pavlov, 2016], concerned with IC origin.

The further adjustment of the model parameters is the subject of the inverse problem, considered in the next section. The proposed approach is quite general and can be easily extended further.

3. Inverse problem

In spite of the fact that from computational point of view the considered evolutionary model is quite simple, being one dimensional in time and radial coordinate, it is still non-linear because of the properties of the liquid metal, forming the core, depend on the temperature, gravity, which in its turn depend on time. Moreover, complexity of the model is concerned with the threshold phenomena: appearance of two new regions where equations change. The first one is already mentioned IC, which origin leads to the change of the turbulent transport of the heat, described by adiabatic law, to the pure conduction of the heat. The other is appearance of the stably stratified layer at the outer part of the liquid core, where the heat flux can be less than the adiabatic, and again, conduction of the heat takes place [In all considered cases in Section 2 stable region at CMB was absent.]. So far the sizes of the both regions can be compared to the size of the liquid core, its influence onto the thermal evolution of the liquid core can be significant.

The mentioned complexity is the reason to explore the full m -dimensional space of parameters, where m is the number of varying parameters. For the large m , that is the case for the considered model, it can be quite difficult problem, even for a small number of constraints n , imposed by observations. As a result special tuning of parameters is needed. Here we present two simple inverse problems of dimension $(m \times n)$, with $m = 3$, $n = 1$ and $n = 2$, solved using the Monte-Carlo method, adopted from the Parker's dynamo simulations, see [Reshetnyak, 2015].

To optimize the selected parameters of the model the following iterative algorithm for the multi-core CPU supercomputer was used. Eqs(3)–(15) were solved numerically with the set \mathcal{P} of the normally distributed over CPU cores random parameters lying in the prescribed ranges. Using MPI, to the end of the current iteration $M = 20$ solutions were obtained, where M was defined by the number of the cores in CPU. To estimate deviation of the

Table 1.

q_b° , mW/m ²	T_o , K	T_s° , K	Ψ_1	$\frac{c - c_m}{c_m}$
0.077	5975	5278	0.01	0.05
0.076	6048	5330	0.03	0.02
0.074	6102	5455	0.0005	0.003
0.054	6102	5267	0.0003	0.001

simulated solution from the desired one the cost-function $\Psi(\mathcal{P})$ was introduced. By definition the less is Ψ the better solution corresponds to observations. The next iteration starts with the new random \mathcal{P} with the mean values of parameters equal to the best choice from the previous iteration and the standard deviation $\sigma = 1$. The iterative process stops when Ψ is less than some fixed value, derived from accuracy of observations, either the number of iterations N reaches maximal threshold.

Firstly we considered $(m \times n) = (3 \times 1)$ problem with varying $\mathcal{P}_1 = (q_b^\circ, T_o, T_s^\circ)$ and constraint, based on the modern radius c_m of IC. The corresponding cost-function has form:

$$\Psi_1(c_m) = 1 - e^{-\mathcal{R}_1}, \quad \mathcal{R}_1 = |c - c_m|. \quad (1)$$

The closer is c to c_m the ‘‘better’’ is the solution.

Using the following ranges of \mathcal{P}_1 $q_b^\circ \in [5 \div 9] 10^{-2}$ mW/m², $T_o \in [5 \div 7] 10^3$ K, $T_s^\circ \in [5.1 \div 5.7] 10^3$ K the evolutionary model was solved $M \times N$ times, where $N \sim 10^4$. The set of the selected solutions after some iterations are listed in the Table 1. The final discrepancy of order 0.1% for c with $q_b^\circ = 0.054$ mW/m² is comparable with accuracy of the seismological observations ~ 1 km [Dziewonski and Anderson, 1981]. Even the previous value, corresponding to the higher value of $q_b^\circ = 0.074$ mW/m², does not look unreasonable.

As was already mentioned, appearance of IC leads to the start of compositional convection in the core, release of the large energy, and as a result to the change of geomagnetic field generation. So far there are no supporting palaeomagnetic observations, we can check possibility that in addition IC is quite old [It is unclear in advance whether the both constraints can be satisfied simultaneously with the desired accuracy.]. Then the cost-function can be modified as follows:

$$\Psi_2(c_m, a) = 1 - e^{-\mathcal{R}_2},$$

Table 2.

q_b° , mW/m ²	T_o , K	T_s° , K	Ψ_2	$\frac{c - c_m}{c_m}$	$\frac{a - \hat{a}}{\hat{a}}$
Case I					
a) 0.051	5648	5486	0.015	0.07	-0.04
b) 0.041	5889	5670	0.0006	-0.006	-0.15
Case II					
a) 0.050	5933	5692	0.007	0.07	-0.05
b) 0.042	5784	5572	$5 \cdot 10^{-5}$	$5 \cdot 10^{-4}$	-0.26
Case III					
a) 0.051	6008	5681	0.0003	-0.003	-0.04
b) 0.041	5383	5184	$3 \cdot 10^{-5}$	$3 \cdot 10^{-4}$	-0.4

$$\mathcal{R}_2 = w_1 |c - c_m| + w_2 \theta(a - \hat{a}) |a - \hat{a}|, \quad (2)$$

where $\theta(a - \hat{a})$ is the Heaviside step function, \hat{a} – the desired time when IC appeared, and $w_1 = w_2 = 0.5$ are the weights. The minimum of Ψ_2 corresponds to $c = c_m$ and IC older than \hat{a} .

We considered three regimes with the same set of parameters and ranges as above and the different \hat{a} : 1, 1.5, 2 Gy, Cases I, II and III, respectively, denoted with the letter ‘‘a’’ in the Table 2.

Only in the Case III, the size of IC c is close to c_m with accuracy 0.3%. The relative accuracy for a is negative -0.04 , that corresponds to IC older than the proposed estimate $\hat{a} = 2$ Gy in 0.08 Gy. Then the age of IC is 2.58 Ga.

As follows from Figure 1 (upper plane), decrease of the heat flux at CMB makes IC older. To demonstrate this we extended range of q_b° to $[4 \div 9] 10^{-2}$ mW/m², see the results in the Table 2, marked by the letter ‘‘b’’. The last two Cases II and III present acceptable accuracy for IC size. In the both Cases a is similar: 1.1 and 1.2 Gy, that corresponds to the age of IC 3.4 and 3.3 Ga, respectively. The estimates in Table 2, give us the range $q_b^\circ = [4 \div 5] 10^{-2}$ mW/m², that corresponds to the modern net heat flux Q at CMB in the range $[5.1 \div 6.4]$ TW. This range lays between estimates of [Gubbins et al., 1979; [Buffett, 2002] and [Calderwood et al., 2003]. This encouraging result allows us to hope that inclusion of additional optimizable parameters and constraints will help to better understanding of the core evolution process.

4. Conclusions

Here we considered only a few parameters and constraints, which of course, do not cover all possibilities. Out of scope left the known problem of the radiogenic elements contribution to the energy budget of the core [Labrosse, 2003]. This problem can be solved using the same inverse approach.

The other skipped above non-trivial problem is what happens with the light constituents rising up from ICB to CMB. Usually, in geodynamo models it is assumed that gradient of light constituents at CMB is negligible, that corresponds to the zero flux of the light constituents at the boundary. In its turn it means that compositional convection is suppressed near CMB. In some sense situation is similar to the thermal convection, where the heat flux decreases as $\sim r^{-2}$, but with the additional Neumann boundary condition.

We also did not consider the case of the large thermal conductivity [Pozzo *et al.*, 2012], which can increase adiabatic heat flux at CMB up to 16 TW, forcing development of the thermally stratified layer at CMB. If in addition conductivity increases with the depth, the thermally stratified layer will develop at ICB as well [Labrosse, 2015]. These scenarios also can be tested using above approach in the future.

The author acknowledges financial support from the Russian Science Foundation (grant No. 19-47-04110).

Appendix

Following [Gubbins *et al.*, 1979], [Labrosse *et al.*, 1997], [Labrosse, 2003] we consider scenario of the Earth's evolution, where soon after the end of the accretion process 4.5 Gy ago, the Earth's core of radius r_b was fully convective. Then, it cooled due to the thermal flux at CMB $r = r_b$, and as a result, depending on the amplitude of the flux q_b , two regions could appear: the solid IC ($0 \leq r \leq c$, region I) and subadiabatic layer in the outer part of the core ($r_1 \leq r \leq r_b$, region III) [Gubbins *et al.*, 1982]. The rest convective part of the core $c \leq r \leq r_1$ here and after is denoted as region II.

Radial distributions of density $\rho(r)$, pressure $P(r)$ and gravity $g(r)$ satisfy to the hydrostatic balance equations:

$$\nabla P = -\rho g, \quad g(r) = \frac{4\pi G}{r^2} \int_0^r \rho(u) u^2 du, \quad (3)$$

with G the gravitational constant. To close system of equations for (P, ρ, g) the logarithmic equation of state is used:

$$P = K_o \frac{\rho}{\rho_o} \ln \frac{\rho}{\rho_o}, \quad (4)$$

where K_o, ρ_o are incompressibility and density at zero pressure, respectively. The optional in the model jump of the density, observed at the surface of the inner core, and which effect on the evolution of the core is quite small, is introduced as follows:

$$\rho(r) = \begin{cases} \rho(r), & \text{if } r \leq c \\ \rho(r) - \delta\rho, & \text{if } r > c. \end{cases} \quad (5)$$

Eqs(3)–(5) with given c we solved numerically, see for details [Reshetnyak, 2019]. Then, with known (P, ρ, g) , adiabatic temperature profile can be derived:

$$T_{ad}(r) = T_c(c) \exp \left(- \int_c^r \frac{\alpha(u)g(u)}{C_p} du \right), \quad (6)$$

where $T_c(c)$ is the temperature at $r = c$, thermal expansion coefficient

$$\alpha(r) = \frac{\gamma C_p \rho_o}{K_o \left(1 + \ln \frac{\rho}{\rho_o} \right)}, \quad (7)$$

with C_p specific heat, and γ for Grüneisen parameter.

If IC is still absent, $c = 0$, then $T_c(c) = T_o$, where the temperature in the center of the Earth T_o can be found from the heat balance equation:

$$4\pi r_1^2 q_1 = -4\pi \int_0^{r_1} \rho C_p \frac{\partial T_{ad}}{\partial t} r^2 dr = -\frac{\partial T_o S}{\partial t}, \quad (8)$$

$$S = 4\pi \int_0^{r_1} \rho C_p \exp \left(- \int_0^r \frac{\alpha g}{C_p} \right) r^2 dr,$$

with q_1 for heat flux density at r_1 . The growth of the inner core starts, when temperature of the liquid core is equal to the temperature of solidification:

$$T_s(r) = T_s^o \left(\frac{\rho(r)}{\rho(c)} \right)^{2(\gamma - \frac{1}{3})}, \quad (9)$$

where T_s° is the temperature of solidification in the center of the Earth. Solidification process starts in the core's center, i.e. $T_c = T_o = T_s^\circ$, $r = c = 0$. Then, for $c > 0$, T_s defines adiabatic temperature at the boundary c in (6): $T_c(c) = T_s(c)$.

Position of the inner core boundary c can be derived from the heat flux equation:

$$r_b^2 q_b - c^2 q_c = \dot{c} (c^2 (P_L + P_G) + P_C), \quad (10)$$

where on the left side is the total heat flux in the region II, and on the right one are the cooling sources, and the dot over c stands for the time derivative.

The latent heat source is defined as

$$P_L(c) = \rho(c) \delta S T_s(c), \quad (11)$$

with δS entropy of crystallization.

Estimate of the release of the gravitational energy due to the growth of the inner core has the form [Loper, 1984]:

$$E_G = \frac{2\pi}{5} G M_o \delta \rho \frac{c^3}{r_b} \left(1 - \left(\frac{c}{r_b} \right)^2 \right), \quad (12)$$

with mass of the core $M_o = 4\pi \int_0^{r_b} \rho(r) r^2 dr$ constant in the model. Then it leads to

$$\dot{E}_G = P_G \dot{c}, \quad P_G = \frac{12\pi}{5} \frac{G M_o \delta \rho}{r_b} c \left(1 - \frac{2c^2}{r_b^2} \right). \quad (13)$$

The main term, concerned with adiabatic cooling, has the form:

$$P_C = - \int_c^{r_1} \rho C_p \frac{\partial T_{ad}}{\partial c} r^2 dr, \quad dc \equiv dr, \quad (14)$$

with q_c heat flux density through the boundary c . Eq(10) was resolved with respect to \dot{c} and then integrated in time. This defines evolution of the inner core boundary c in time.

From condition of continuity of the temperature at the boundary c , follows that $T_s(c)$ is the boundary condition for the thermal-diffusion equation in the region $0 < r < c$, I, with a moving boundary $c(t)$ [Kutluay, 1997]:

$$\frac{\partial T}{\partial t} = k \Delta T, \quad (15)$$

where k is the thermal diffusivity. The second boundary condition in the center $r = 0$ is $T' = 0$,

Table 3.

Parameter	Value
G	$6.6873 \cdot 10^{-11} \text{ m}^3/(\text{kg s}^2)$
k	$7 \cdot 10^{-6} \text{ m}^2/\text{s}$
ν	$10^{-6} \text{ m}^2/\text{s}$
λ	$10^{-9} \text{ m}^2/\text{s}$
β	1
γ	1.5
r_b	3480 km
δS	118 J/(kg K)
ρ_o	7500 kg/m ³
$\delta \rho$	500 kg/m ³
T_s°	5270 K
T_o	6000 K
K_o	$4.76 \cdot 10^{11} \text{ Pa}$
C_p	860 J/(kg K)

where ' is a derivative on r . The joined system (3) – (15) defines evolution of the fields in the regions I and II.

If the adiabatic heat flux density $q_{ad}(r) = -\kappa T'_{ad}(r)$, with thermal conductivity $\kappa = k\rho C_p$, becomes larger than the heat flux density at the outer boundary r_b : $q_{ad}(r) < \left(\frac{r_b}{r}\right)^2 q_b$, the sub-adiabatic stably stratified thermal region III develops at the outer part of the core, where the heat flux density is smaller. The temperature profile in the region III can be derived from Eq(11) with the moving boundary $r_1(t)$, and two boundary conditions: $T(r_1) = T_{ad}(r_1)$ at the inner boundary, and given heat flux density $q_b(t)$ at the outer boundary r_b . In the general case Eqs(3)–(15) in regions I–III are solved numerically, using iterative methods with under-relaxation method to provide numerical stability. The numerical values of parameters are listed in the Table 3.

The developed MPI C++ code provides possibility to solve equations for the set of parameters simultaneously, as well as to solve the inverse problem using the Monte-Carlo method, similar to [Reshetnyak, 2015]. The Matplotlib Python library was used for graphics. The 40-cores workstations Intel(R) Xeon(R) CPU E5-2640 with Gentoo OS were used for simulations.

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